

6.4 Exercises

Log Review Sheet

① $2^{3x} = 32$
 $2^{3x} = 2^5$
 $3x = 5$
 $x = 5/3$

② $3^{-2} = 2c$
 $\frac{1}{9} = 2c$
 $\frac{1}{18} = c$

③ $(2x)^{-2} = 16$
 $\frac{1}{4x^2} = 16$
 $1 = 64x^2$
 $\frac{1}{64} = x^2$
 $\frac{1}{8} = x$

④ $25^{1/2} = \frac{x}{2}$
 $5 = \frac{x}{2}$
 $10 = x$

⑤ $4^2 = 5x + 1$
 $16 = 5x + 1$
 $15 = 5x$
 $3 = x$

⑥ $8^{2/3} = x - 5$
 $4 = x - 5$
 $9 = x$

⑦ $3x - 1 = 2x + 3$
 $x = 4$

⑧ $x^2 - 6 = 2x + 2$
 $x^2 - 2x - 8 = 0$
 $(x - 4)(x + 2) = 0$
 $x = 4$ ~~$x = -2$~~

⑨ $(x + 4)^3 = 27$
 $x + 4 = 3$
 $x = -1$

⑩ $2^4 = x + 3$
 $16 = x + 3$
 $13 = x$

⑪ $x^3 = 1000$
 $x = 10$

⑫ $8^2 = 4x + 4$
 $64 = 4x + 4$
 $60 = 4x$
 $15 = x$

⑬ $x = 12$

⑭ $x - 5 = 13$
 $x = 18$

⑮ $x = 5x - 20$
 $-4x = -20$
 $x = 5$

⑯ $x = 2x - 1$
 $-x = -1$
 $x = 1$

⑰ $x + 12 = 4x$
 $12 = 3x$
 $4 = x$

⑱ $x - 3 = 2x$
 $-3 = x$

19 $2x > 2^2$
 $2x > 4$
 $x > 2$

20 $x > 5^2$
 $x > 25$

21 $3x+1 < 2^4$
 $3x+1 < 16$
 $3x < 15$
 $0 < x < 5$

22 $2x > 4^{-1/2}$
 $2x > \frac{1}{2}$
 $x > 1$

23 $(x+3) < 3^3$
 $x+3 < 27$
 $0 < x < 24$

24 $6x > 27^{2/3}$
 $6x > 9$
 $x > \frac{3}{2}$

25 $5x < 30$
 $0 < x < 6$

26 $x < 2x-4$
 $-x < -4$
 $x > 4$

27 $3x < 7x-8$
 $-4x < -8$
 $x > 2$

28 $8x+5 > 9x-18$
 $-x > -23$
 $2 < x < 23$

$8x+5 > 0$ $9x-18 > 0$
 $8x > -5$ $9x > 18$
 $x > -\frac{5}{8}$ $x > 2$

29 $3x+7 < 7x-3$
 $-4x < -10$
 $x > \frac{5}{2}$

30 $3x-4 < 2x+7$
 $\frac{4}{3} < x < 11$

$3x-4 > 0$ $2x+7 > 0$
 $3x > 4$ $2x > -7$
 $x > \frac{4}{3}$ $x > -\frac{7}{2}$

* 31

$\log_2 10^3$
 $3 \log_2 10$

$2^4 = 10^3$

Name Key Date _____ Period _____

The Meaning Of Logarithms

Rewrite each equation in exponential form.

1) $\log_6 36 = 2$

$6^2 = 36$

3) $\log_{14} \frac{1}{196} = -2$

$14^{-2} = \frac{1}{196}$

Rewrite each equation in logarithmic form.

5) $64^{\frac{1}{2}} = 8$

$\log_{64} 8 = \frac{1}{2}$

7) $9^2 = \frac{1}{81}$

$\log_9 \frac{1}{81} = -2$

Rewrite each equation in exponential form.

9) $\log_{\frac{15}{16}} x = y$

$\frac{15}{16}^y = x$

11) $\log_{\frac{7}{4}} x = y$

$\frac{7}{4}^y = x$

13) $\log_u v = -16$

$u^{-16} = v$

Rewrite each equation in logarithmic form.

15) $a^{14} = v$

$\log_a v = 14$

2) $\log_{289} 17 = \frac{1}{2}$

$289^{\frac{1}{2}} = 17$

4) $\log_3 81 = 4$

$3^4 = 81$

6) $12^2 = 144$

$\log_{12} 144 = 2$

8) $\left(\frac{1}{12}\right)^2 = \frac{1}{144}$

$\log_{\left(\frac{1}{12}\right)} \frac{1}{144} = 2$

10) $\log_u u = 4$

$u^4 = u$

12) $\log_2 v = u$

$2^u = v$

14) $\log_y x = -8$

$y^{-8} = x$

16) $8^6 = a$

$\log_8 a = 6$

17) $\left(\frac{1}{3}\right)^{-y} = x$

$\log_{\frac{1}{3}} x = y$

19) $9^x = x$

$\log_9 x = y$

20) $6^x = 123$

$\log_6 123 = a$

Evaluate each expression.

21) $\log_4 64$

3

22) $\log_6 216$

3

23) $\log_4 16$

2

24) $\log_3 \frac{1}{243}$

-5

25) $\log_5 125$

3

26) $\log_2 4$

2

27) $\log_{343} 7$

$\frac{1}{3}$

28) $\log_2 16$

4

29) $\log_{64} 4$

$\frac{1}{3}$

30) $\log_6 \frac{1}{216}$

-3

Simplify each expression.

31) $12^{\log_3 144}$

144

32) $5^{\log_5 17}$

17

33) $x^{\log_3 2}$

72

34) $9^{\log_3 20}$

400

$3^2 \log_3 20$

$3 \log_3 20^2$